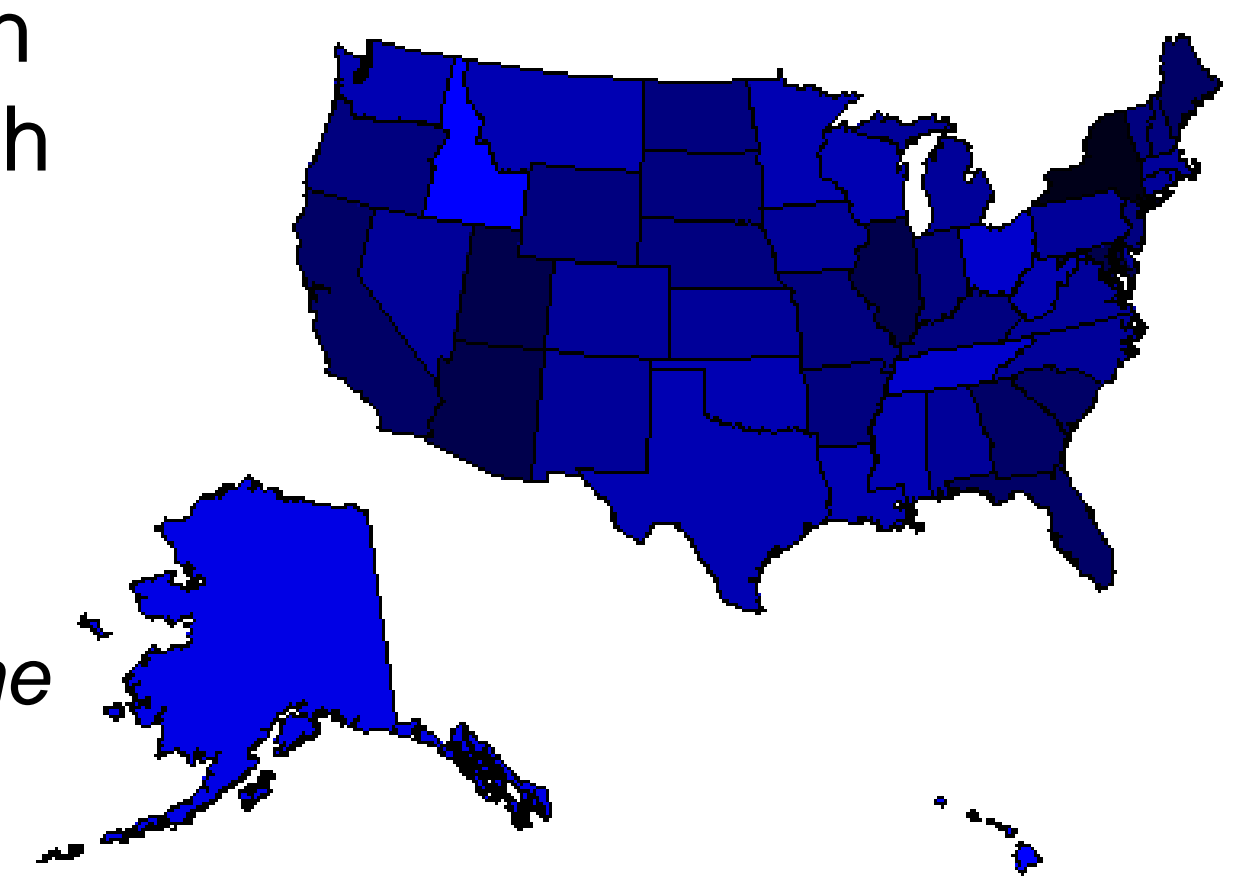


Yixiao Sheng, Yu-Chung Lien, Ching-Hua Wang

### Problem

How many years it takes, for people with different race, education, gender, English speaking ability etc., to be granted their naturalizations? Our project focus on people who lives in California.



The US map shows the average length of time for immigrants to become American citizens over 5,000,000 samples

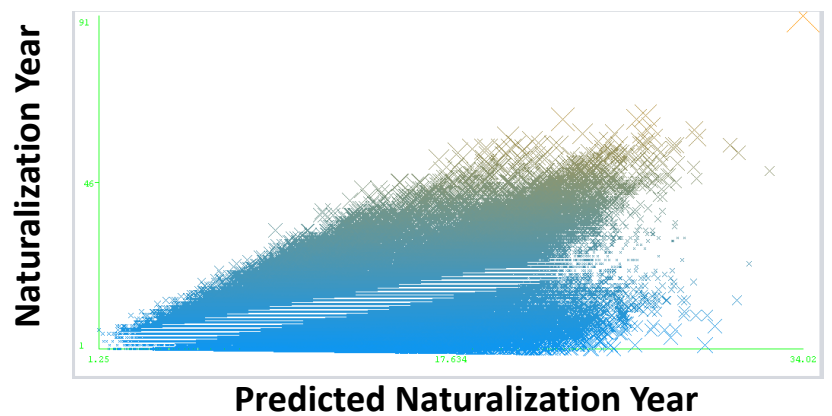
### Dataset

American Community Survey 2008-1013

### Linear Regression

$$h(x) = \sum_{i=0}^n \theta_i x_i = \theta^T x$$

$$J(\theta) = \frac{1}{2} \sum_{i=1}^m h_{\theta}(x^{(i)}) - y^{(i)}^2$$

$$\theta_j := \theta_j + \alpha \sum_{i=1}^m (y^{(i)} - h_{\theta}(x^{(i)})) x_j^{(i)}$$


Features	Weights
Year of entry	-30.3
Age	-4.2
Wage income	-0.4
Disability	0.4
Gender	0.2

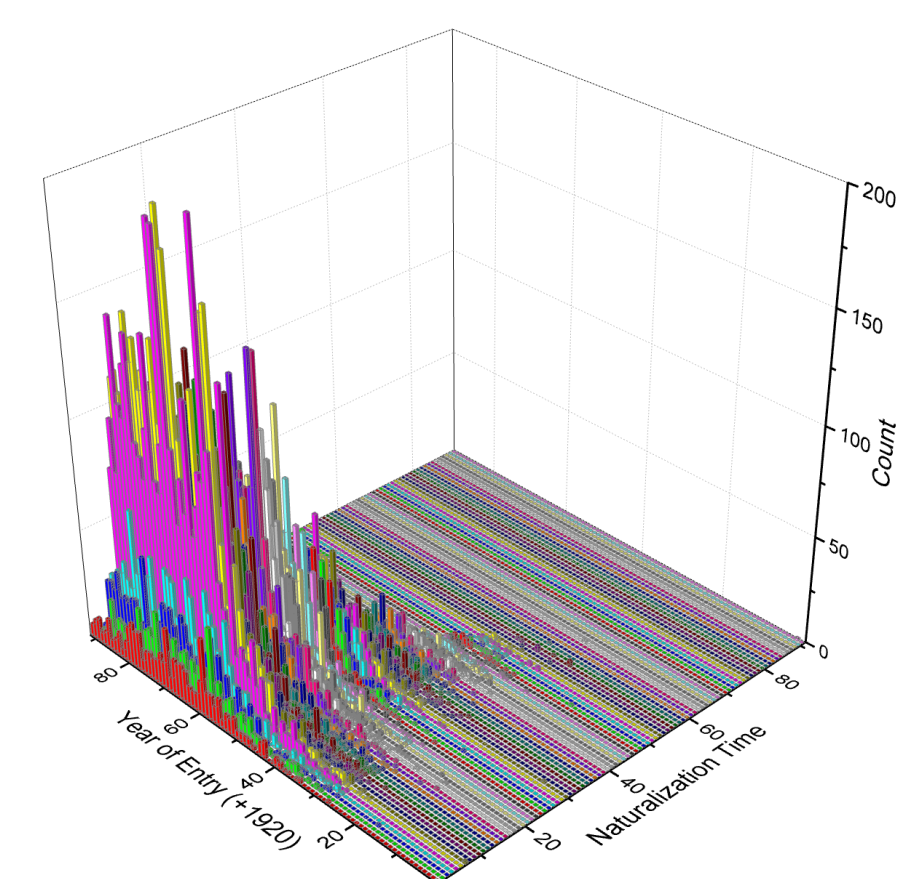
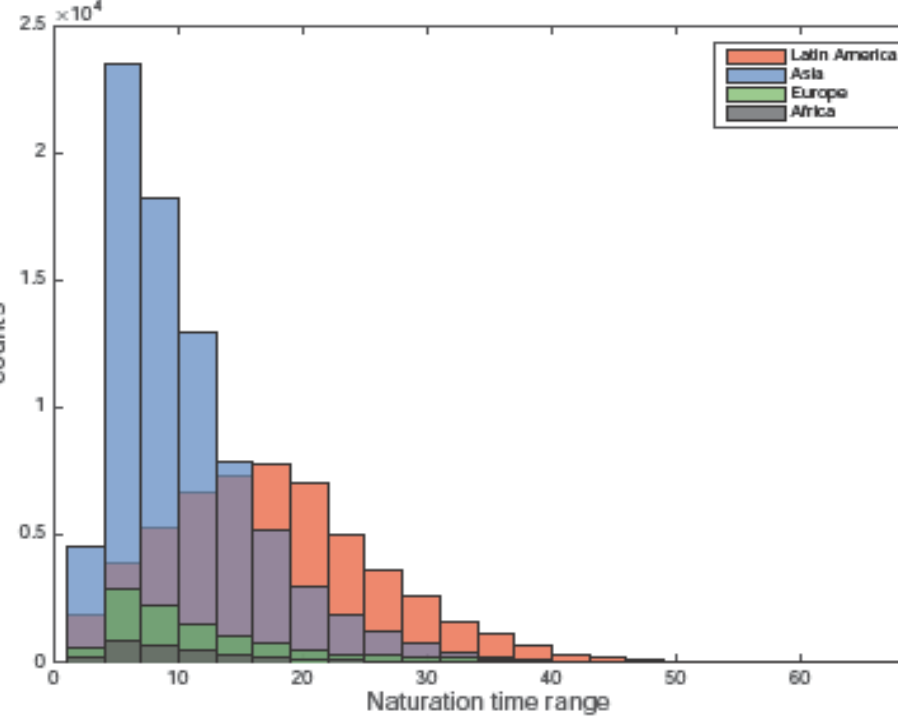
World Area of Birth	Weights
Born in Latin America	1.4
Born in Asia	-2.9
Born in Europe	-2.9
Born in Africa	-2.2
Born in Northern America	-0.9
Oceania and at Sea	-1.6

Educational attainment	Weights
Below 12th grade - no diploma	-1.1
Below college	-2.5
Associate's degree	-3.3
Bachelor's degree	-3.0
Master's degree	-2.4
Professional degree beyond a bachelor's degree	-3.4
Doctorate degree	-1.6

Ability to speak English	Weights
Very well	0.1
Well	0.8
Not at all	2.3

The table highlights the features that contribute to faster naturalization.

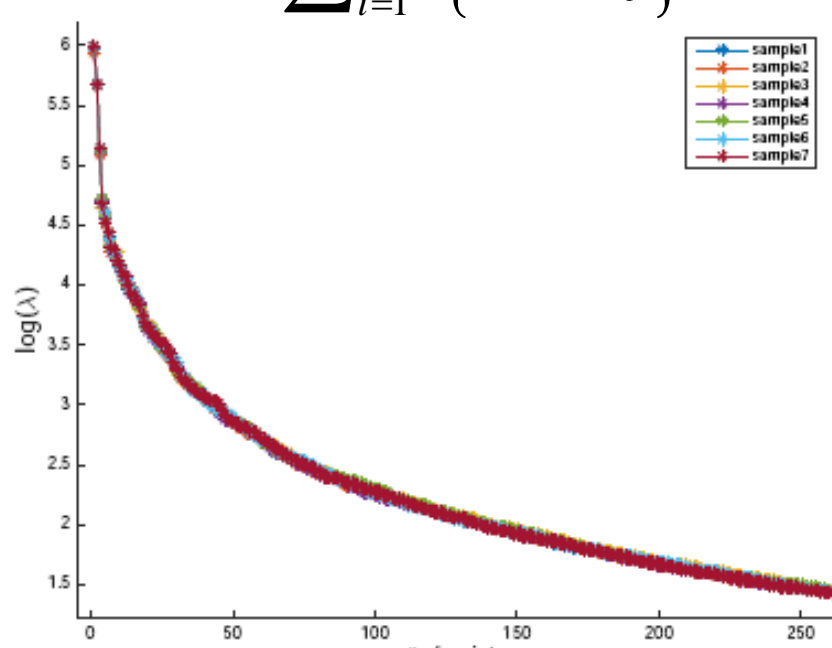
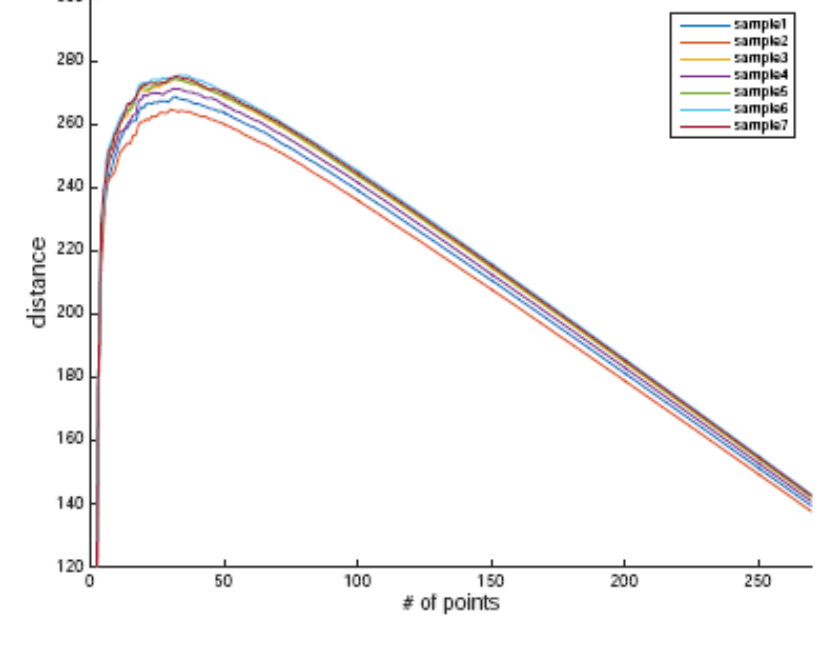
### Statistic Distribution

- The statistical distribution of Year of entry v.s. naturalization time.
- World area of birth versus naturalization time.

### Kernal Matrix Analysis & K-Means Cluster

$$c^{(i)} = \arg \min_{\theta} \|x^{(i)} - \mu_j\|^2$$

$$\mu_j := \frac{\sum_{i=1}^m 1\{c^{(i)} = j\} x^{(i)}}{\sum_{i=1}^m 1\{c^{(i)} = j\}}$$



Use sorted eigenvalue from Gaussian kernel matrix versus data points and distance versus data points to determine the number of groups.

Group Number (Male)		1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
World Area of Birth	Latin America	v	v	v						v							
	Africa															v	
	Asia				v	v	v	v	v	v	v	v	v				v
Race	White			v								v				v	
	Black				v												
	Others			v													
Marital Status	Married		v	v			v	v	v	v	v	v	v	v	v	v	v
	Never Married	v															
English Speaking Ability	Separated				v									v			
	Good	v	v	v	v	v	v	v	v	v	v	v	v	v	v	v	v
Class of Worker	Not Good											v					
	Private Company	v	v	v						v	v	v					v
Education Attainment	Government				v					v	v	v					
	High School or Lower			v	v					v	v	v	v				v
	Bachelor Degree								v								v
Age at time of Entry	Master or Higher																v
	Young	v								v							v
Income	Low										v						
	High															v	v
Naturalization	Long	v	v	v												v	v

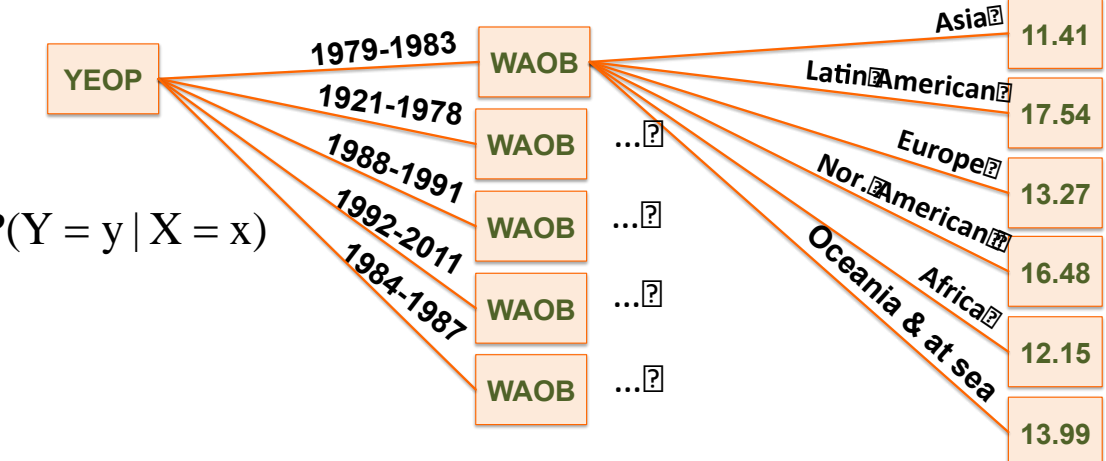
Group Number (Female)		1	2	3	4	5	6	7	8	9	10	11	12	13	14		
World Area of Birth	Latin American						v			v							
	Asian		v	v	v			v	v	v	v				v		
	White				v												
Race	Black																
	Others																
	Married	v	v				v	v	v					v	v		
Marital Status	Never Married		v														
	Separated									v		v					
Female have children under 17	With Children						v	v	v					v	v		
	No Children																
English Speaking Ability	Good	v	v		v		v	v	v	v	v	v	v	v	v		
	Not Good																
Class of Worker	Private Company		v				v										v
	Government							v									
Education Attainment	High School or Lower		v	v	v	v				v							
	Bachelor Degree																v
	Master or Higher		v														
Age at time of Entry	Young	v			v							v				v	
	Low																
Income	High																
	Long																

### Decision Regression

$$H(Y|X) = \sum_x P(X=x) H(Y|X=x)$$

$$= -\sum_x P(X=x) \sum_y P(Y=y|X=x) \log_2 P(Y=y|X=x)$$

$$= -\sum_{x,y} P(X=x, Y=y) P(Y=y|X=x)$$

$$IG(X) = H(Y) - H(Y|X)$$


- Features selection optimization was implemented to achieve correlation 0.595.
- The important features match linear regression result.

Number of Features	Feature	Correlation Coefficient	Size of Tree
1	Year of Entry	0.4252	6
	Arrive Age	0.2652	8
	Education Level	0.2091	4
	World Area of Birth	0.4141	7
	English Level	0.0924	5
2	Race	0.3513	7
	Year of Entry	0.5749	36
3	World Area of Birth		
	Year of Entry		
	WAOB	0.5817	105
4	Education Level		
	Year of Entry		
	World Area of Birth	0.591	475
	Arrive Age		
5	Education Level		
	Year of Entry		
	World Area of Birth		
	Arrive Age	0.596	958

### Conclusion

- The clustering results indicate that people from Asia with higher degree need longer naturalization time. However, the linear regression shows generally, higher degree actually contribute to faster process. As world area of birth also plays a major roll, we use regression tree to reveal more details.
- The large weight of year of entry and world area of birth match well with the statistical distribution
- After using decision regression, the correlation coefficient improves from 0.56 to 0.59.

### Reference

- [http://www2.census.gov/acs2013\\_1yr/pums/csv\\_pus.zip](http://www2.census.gov/acs2013_1yr/pums/csv_pus.zip)
- [https://en.wikipedia.org/wiki/Determining\\_the\\_number\\_of\\_clusters\\_in\\_a\\_data\\_set](https://en.wikipedia.org/wiki/Determining_the_number_of_clusters_in_a_data_set)
- <https://alliance.seas.upenn.edu/~cis520/wiki/index.php?n=Lectures.DecisionTrees>