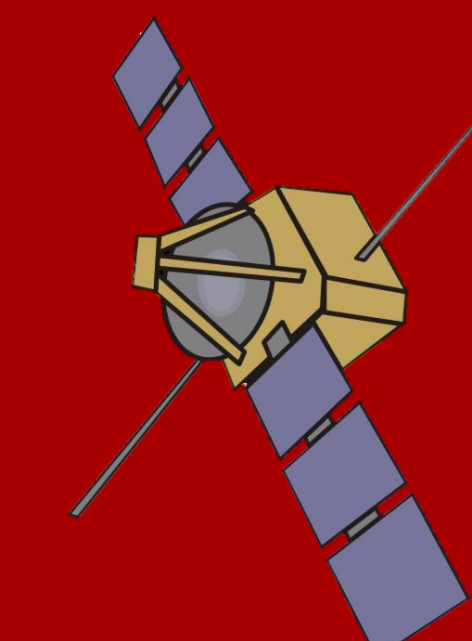




Satellite Anomaly Prediction using Survival Analysis and Machine Learning Approaches



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Introduction

Satellites and space systems are integral to processes such as communication and navigation but are under constant threat from the space environment. As a result, agencies such as NOAA have monitored satellites and recorded hundreds of anomalous behaviors [1] [2]. Here we attempt to use this data with survival analysis and machine learning approaches to predict the time to a satellite anomaly. In the end, we found that the approaches considered did not work well with the limited and noisy data set

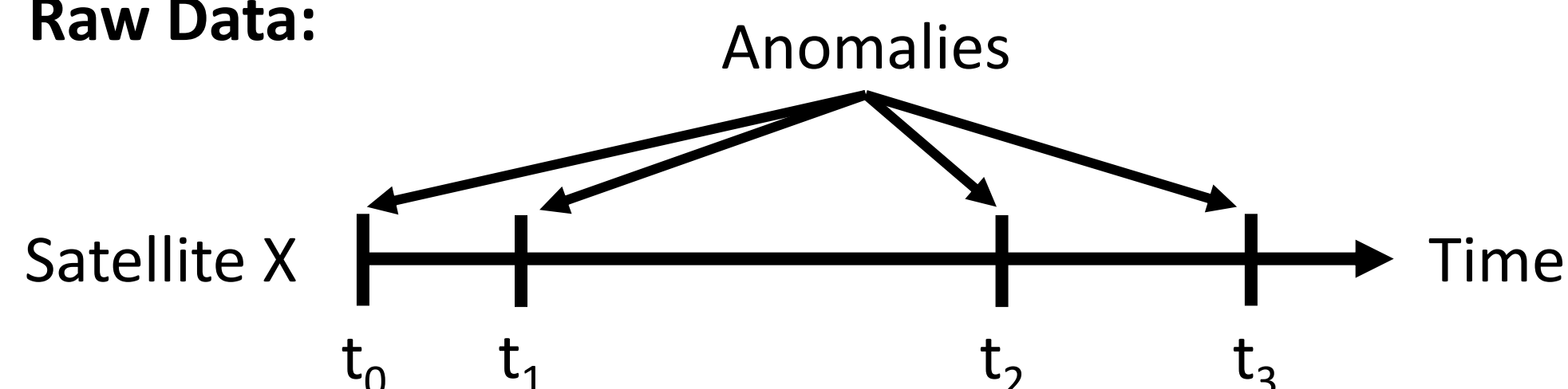
Data Processing

Raw data = Satellite names with anomaly timestamps

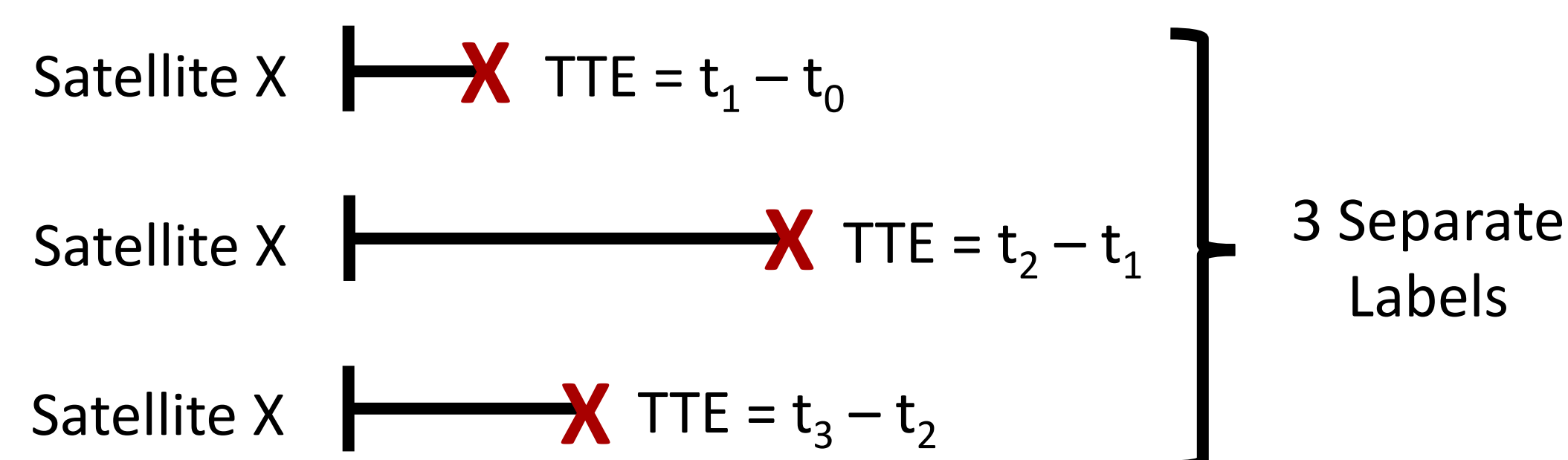
Goal: Pose problem as a “Time to Event” (TTE) prediction

- Classical treatment predicts time until patient death
- Treat each anomaly as an independent “patient”

Raw Data:



Processed Data:

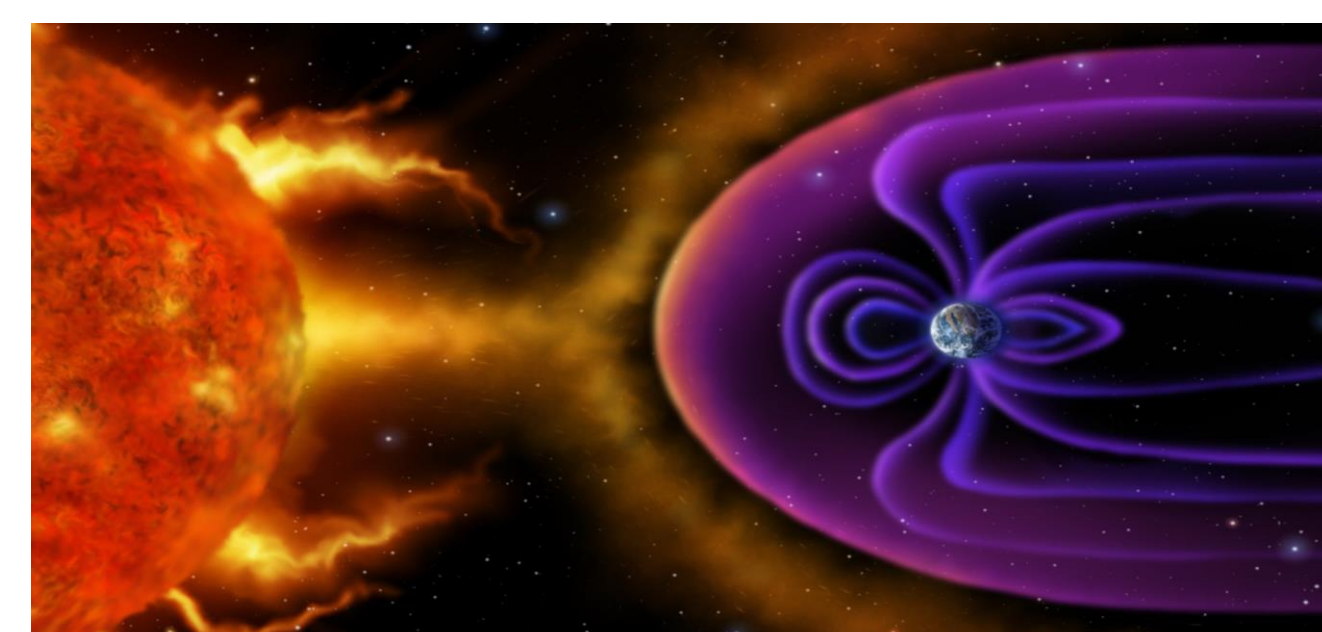


Data & Features

Processed dataset has **726 datapoints** for 10 satellites
 - Anomalies recorded between 1976 and 1994

6 features:

- Starting Month* = Position of earth around sun
 - Sun-Spot Number* = Measure of solar activity
 - X-ray Flux* = Count of high energy particles
 - Mass* = Size of spacecraft
 - Perigee* = Distance from earth
 - Inclination* = Tilt of orbit
- Space Conditions (grouped with Starting Month, Sun-Spot Number, X-ray Flux)
 Spacecraft attributes (grouped with Mass, Perigee, Inclination)

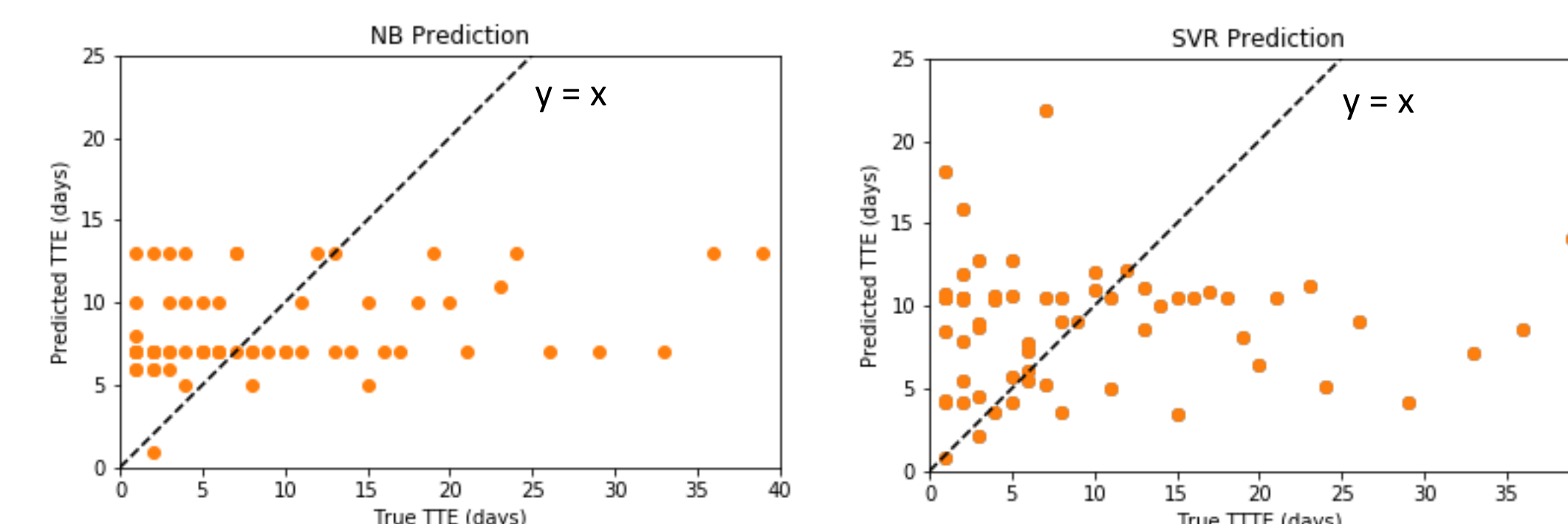


Results

Used k-fold cross validation with k=10 to evaluate

Training Set = 654 points Test Set = 72 points

Model	Training Set Mean Error	Test Set Mean Error
Linear Regression	455%	475%
Naïve Bayes	100%	167%
Support Vector Regression	65%	190%



Models

Linear Regression: Initial baseline results

Support Vector Machine: Use RBF kernel to capture nonlinearities

$$\min_{W,b} \frac{1}{2} \|W\|^2 + C \sum_{i=1}^n (\xi_i + \xi_i^*) \quad \text{constrained by} \quad \begin{aligned} y_i - (w^T \phi(x_i) + b) &\leq \epsilon + \xi_i \\ (w^T \phi(x_i) + b) - y_i &\leq \epsilon + \xi_i^* \\ \xi_i, \xi_i^* &\geq 0, \quad i = 1 \dots n \end{aligned}$$

Naïve Bayes: Perform classification each time step until failure

$$p(y = 1|x) = \frac{(\prod_{j=1}^d p(x_j|y = 1)) p(y = 1)}{(\prod_{j=1}^d p(x_j|y = 1)) p(y = 1) + (\prod_{j=1}^d p(x_j|y = 0)) p(y = 0)}$$

$$p(y = 1) = S(t) = \prod_{i=1}^m \left(1 - \frac{1}{r_i}\right) = \text{Kaplan - Meier estimator}$$

Discussion

- Machine Learning models did not adequately predict the satellite anomalies
- Most likely other factors were not being accounted for (e.g. space debris, geometry, etc.)
- Naïve Bayes might improve without Gaussian assumption
- Support vector regression was best on training set, but consistently overfit the training data

References

[1]: Wolfson (1993). *Satellite Anomalies*, electronic dataset, NOAA
 [2]: Wilkinson et al. (1991). *TDRS-1 Single Event Upsets and the Effect of the Space Environment*. IEEE Transactions on Nuclear Science, Vol 38, No. 6
 [3]: Wolfson et al. (2015). *A Naïve Bayes machine learning approach to risk prediction using censored, time-to-event data*. Stat Med